

Let  $C$  be a site,  $C^\wedge$  the category of presheaves on  $C$  and  $C^\sim$  the category of sheaves on  $C$ .

It is well known that the inclusion functor  $i : C^\sim \rightarrow C^\wedge$  has a left adjoint functor  $a : C^\wedge \rightarrow C^\sim$ , which is called the sheafification functor. The functor  $a$  is defined by  $a = L^2$  where  $L : C^\wedge \rightarrow C^\sim$  is a functor which assigns a separated presheaf to each presheaf.

On the other hand, the existence of a left adjoint of the inclusion functor  $i$  can be considered as an orthogonal subcategory problem in general category theory. From this point of view, the left adjoint is constructed using a certain functor  $\Delta : C^\wedge \rightarrow C^\wedge$ .

In this talk, we study the relation between these two constructions and show that the two functors  $L$  and  $\Delta$  are naturally isomorphic.